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# **A Deterministic Modeling Approach for Estimating Recharge in South Washington County**

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# Acknowledgements

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## **Consortium of Sponsors include:**

Washington County

City of Afton

City of Woodbury

Valley Branch Watershed District

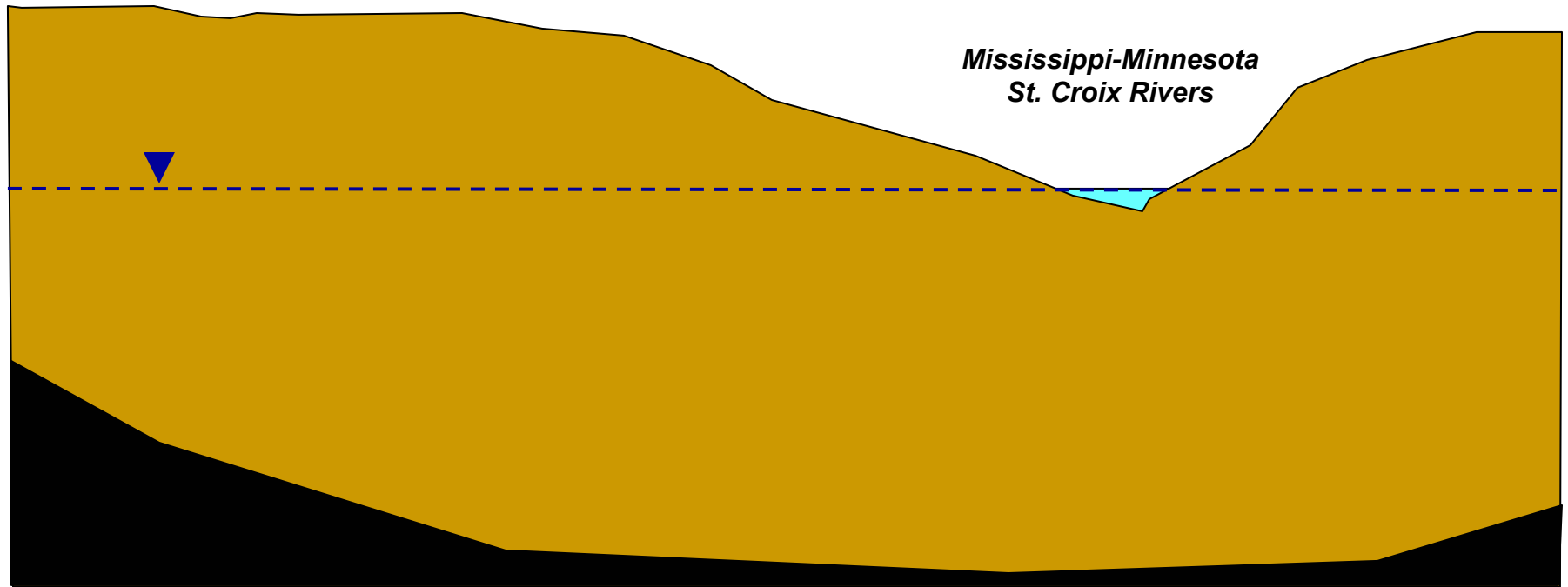
South Washington Watershed District



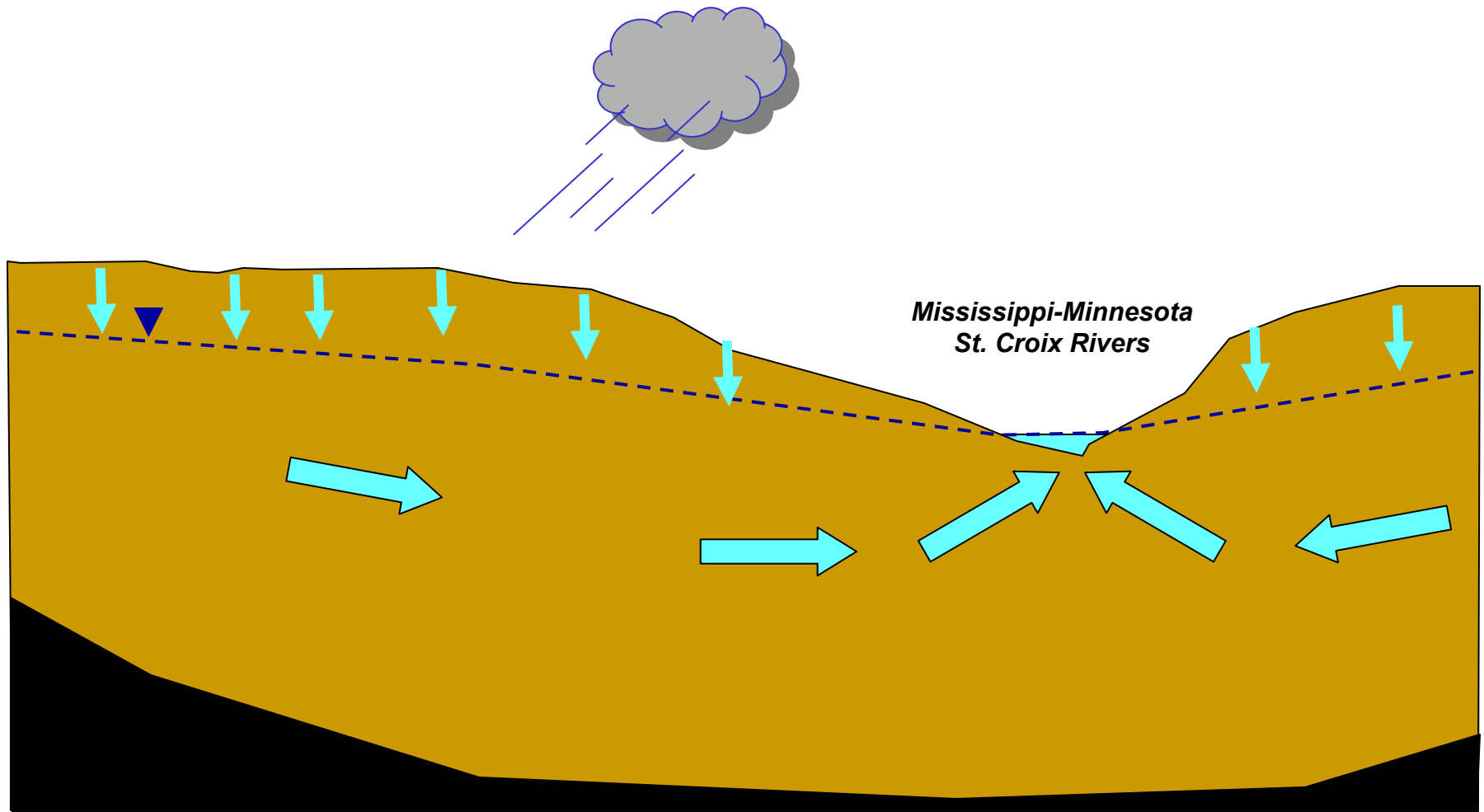
# This talk addresses:

- “Traditional” approaches used to estimate recharge for groundwater flow models
- The contribution of recharge estimates to model uncertainty
- A deterministic approach to modeling the recharge process
- An example from southern Washington County
- Problems and challenges of this approach

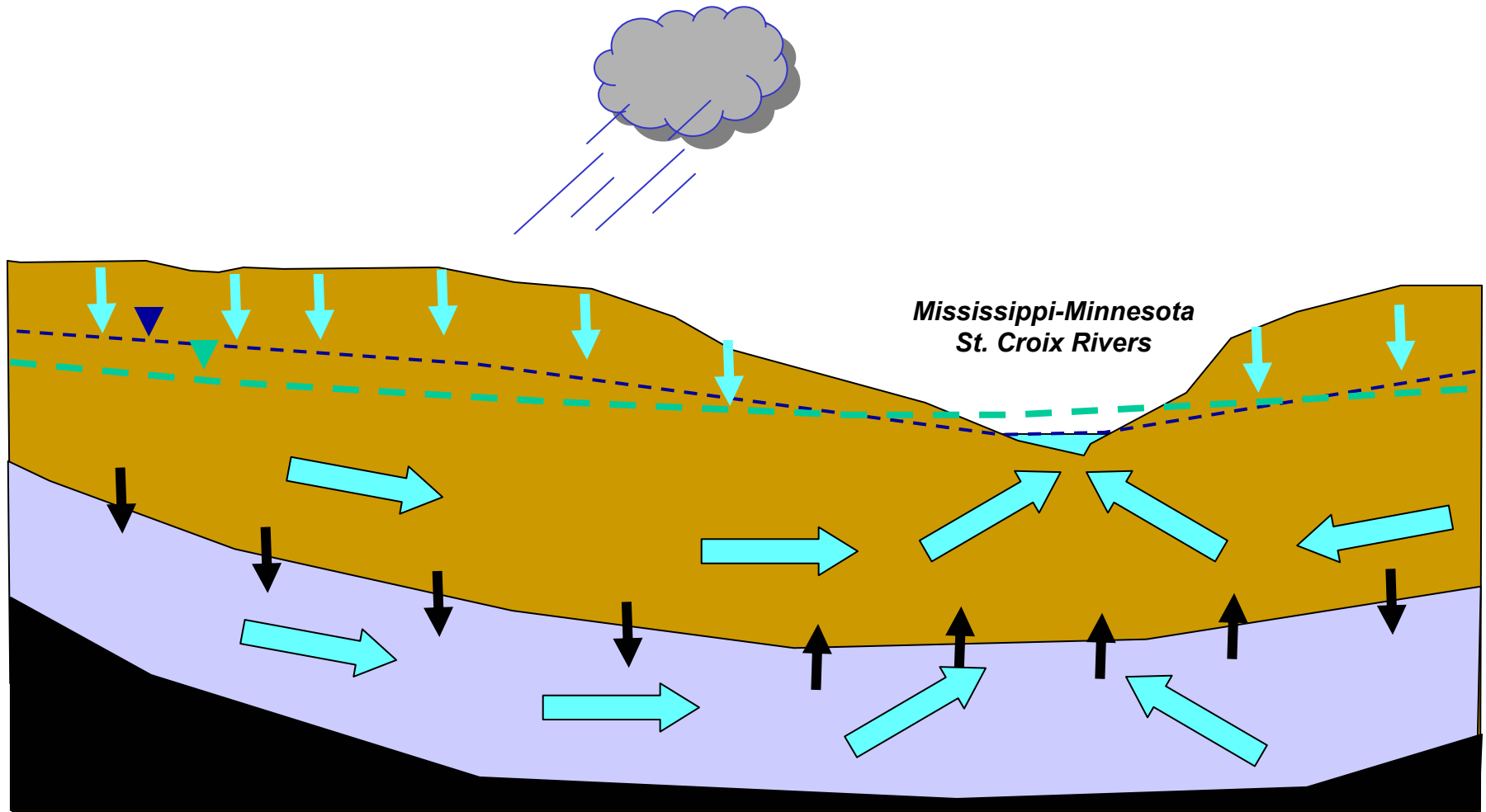
## In the Absence of Recharge the Potentiometric Surfaces Would be Flat

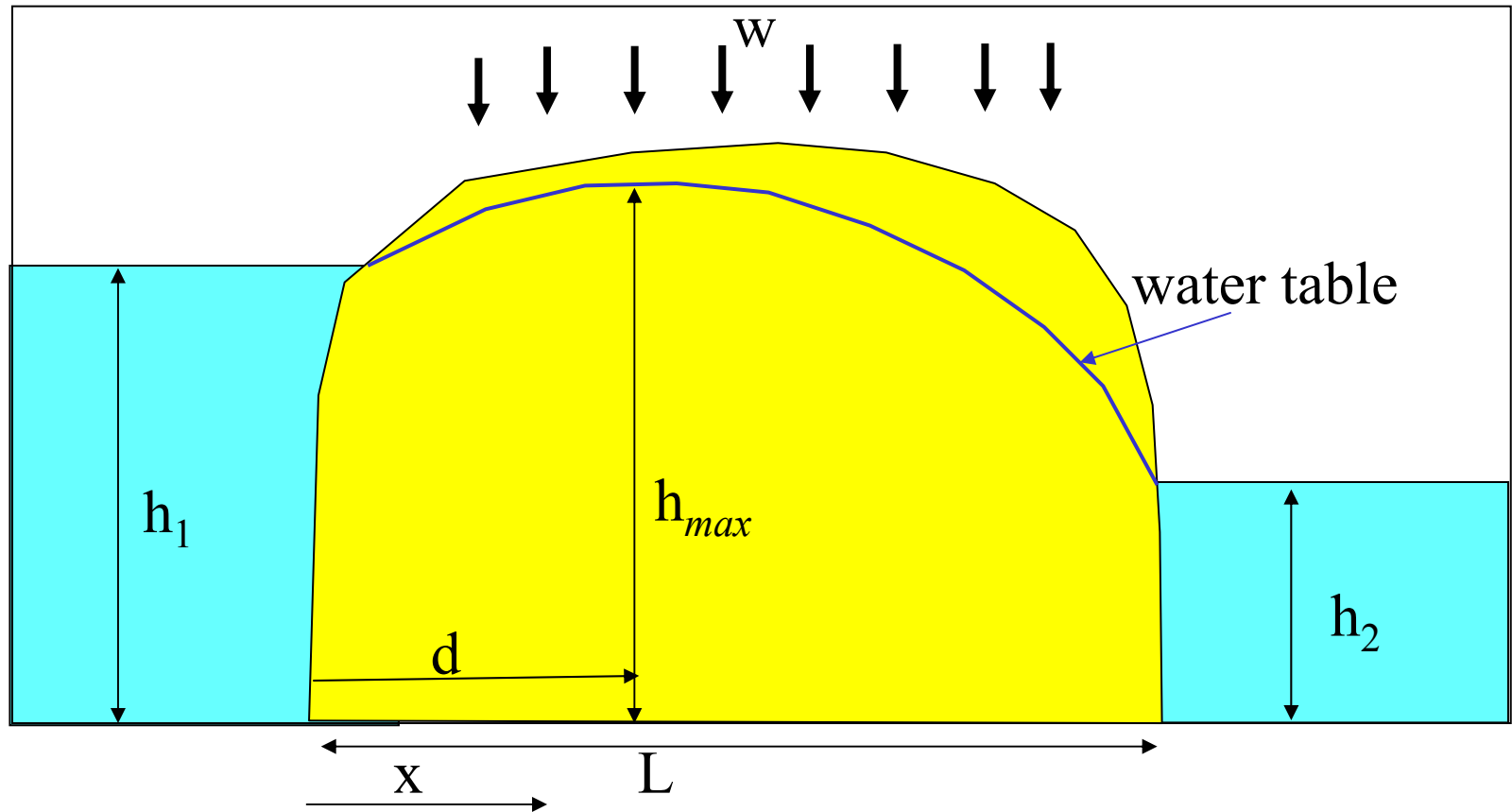


## Recharge Causes the Potentiometric Surface to Rise and Groundwater to Flow



# Leakage in a Multi-Aquifer System Distributes Recharge to Deeper Aquifers and Effects Potentiometric Surfaces

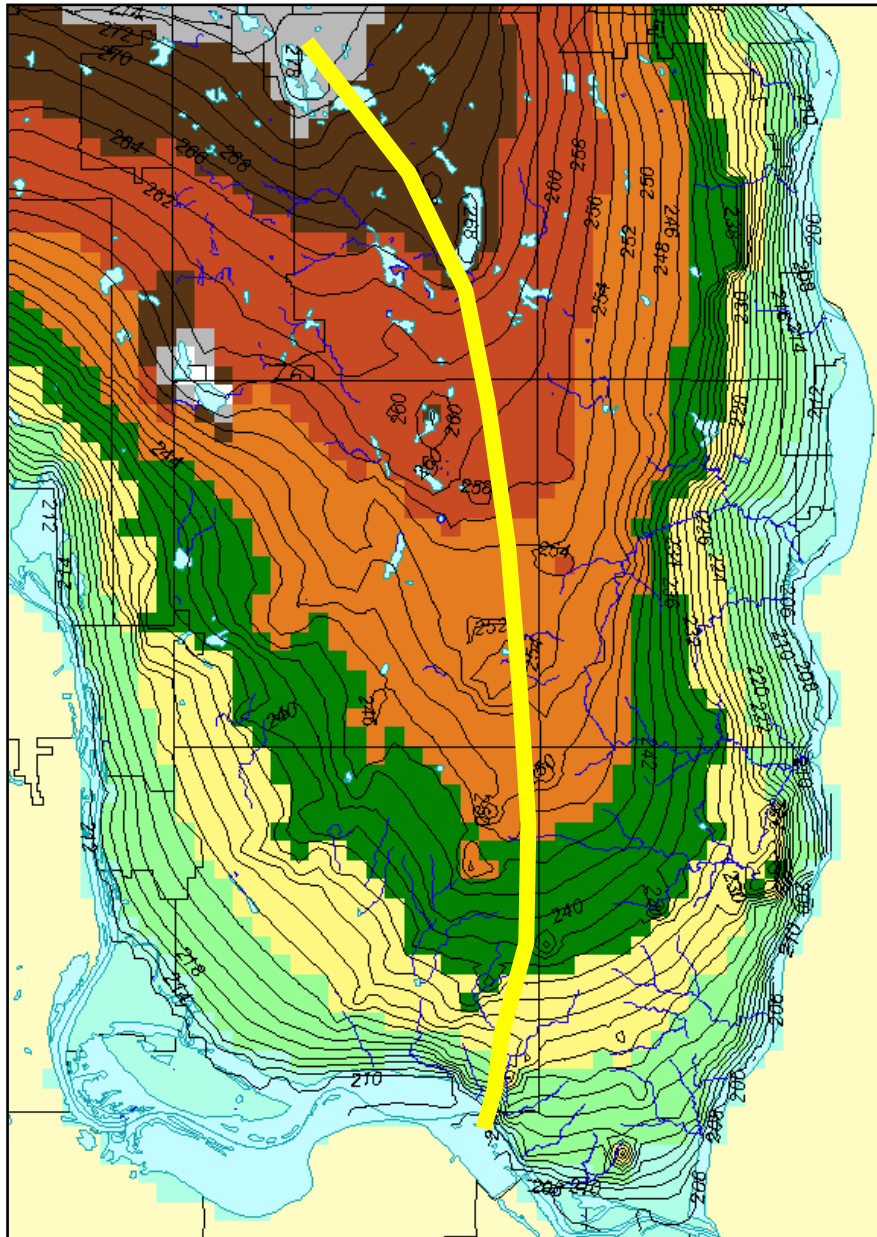




$$h = \sqrt{h_1^2 - \frac{(h_1^2 - h_2^2)x}{L} + \frac{w}{K}(L-x)x}$$

**Dupuit Equation**

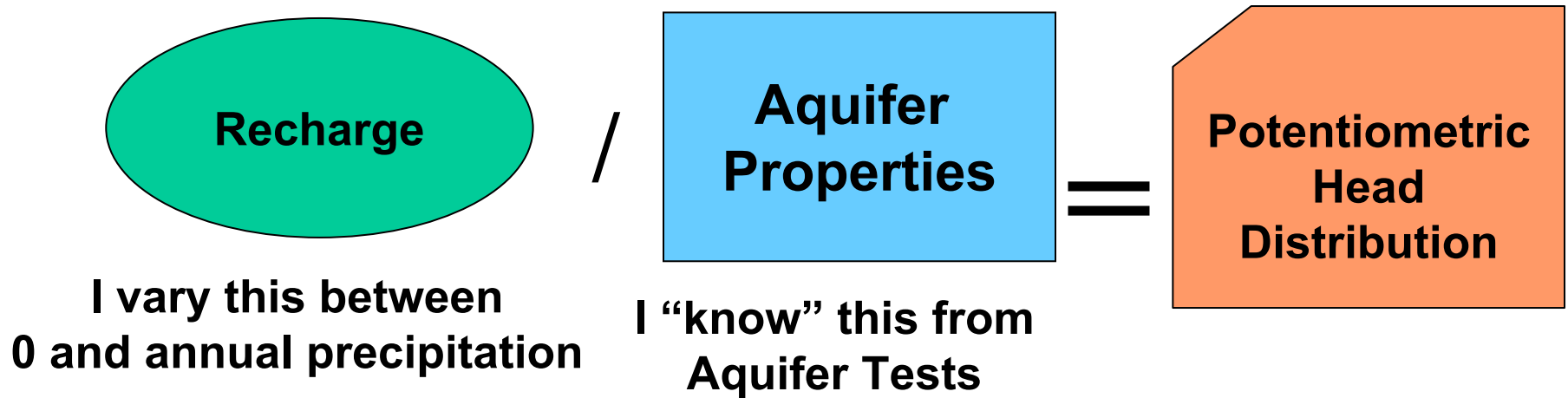
**Head is dependent on the ratio of Recharge to permeability**



## Southern Washington County in Geometrically Similar to a “Dupuit” Problem



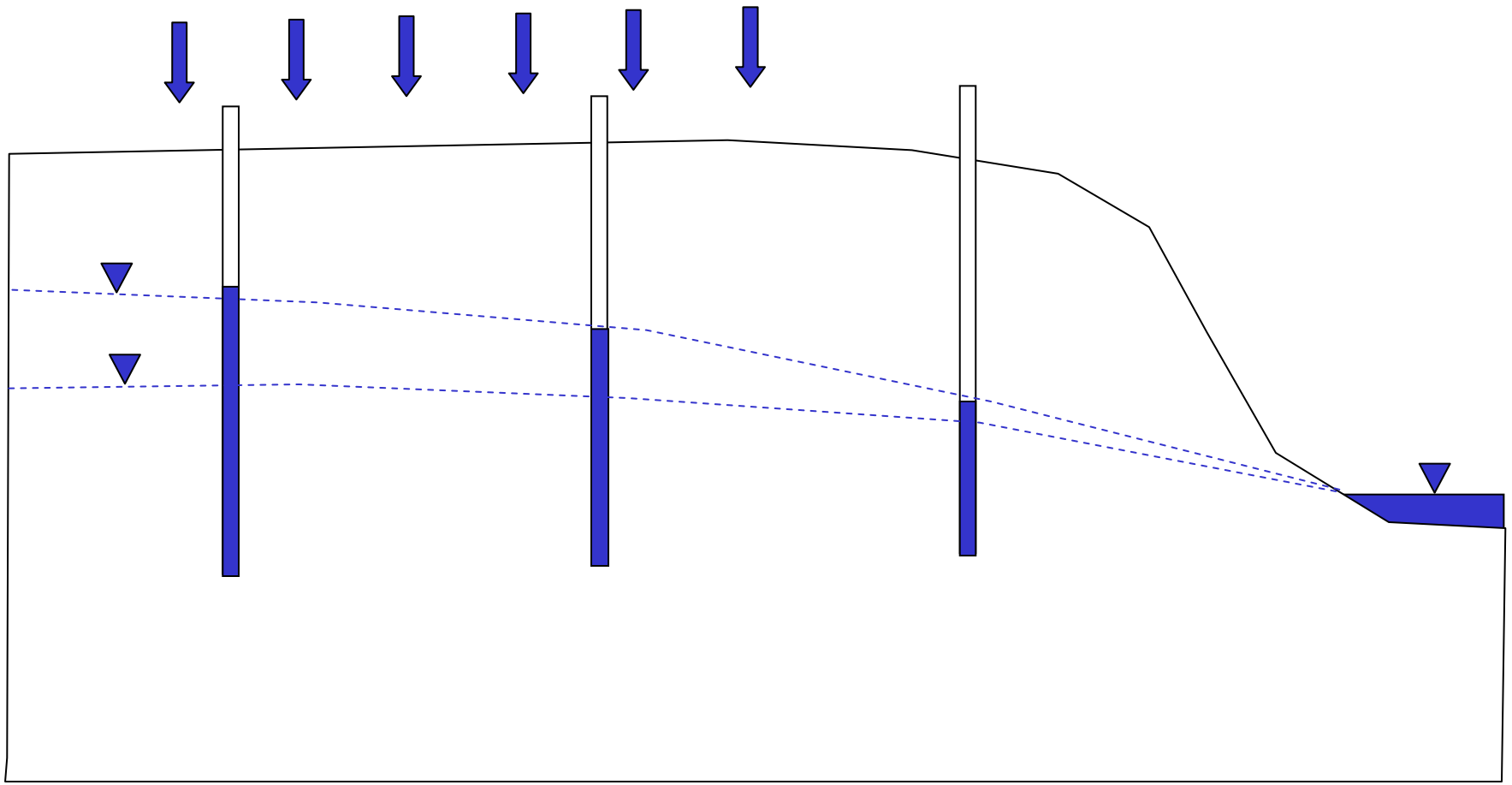
# Estimating Recharge by the “Inverse Problem” Approach



# **Inverse Method Depends on Having a Higher Confidence in Transmissivity Values of Aquifers than in Recharge Estimates**

- “I can reliably estimate transmissivity from pumping tests”
- “I can draw contour maps of aquifer thickness”
- “I can contour potentiometric heads from well data”
- “Recharge rates must be bounded between 0 and @ 30 inches per year”

# Recharge Values are Adjusted (and distributed over areas) Until Simulated Heads Match Measured Ground-Water Levels



Estimates Range from 4 to 12 inches per year (Average about 8-9 inches per year)

# There is inherent uncertainty in such recharge estimates

- Depends on transmissivity estimates
- Depends on how many (and how) aquifers and aquitards are included in a model
- Depends on model extent and boundary conditions
- Depends on how sources or sinks are represented in models

**There is an inherent lack of uniqueness in inverse modeling approaches**

# New Problems Have Increased the Interest in Recharge Estimation

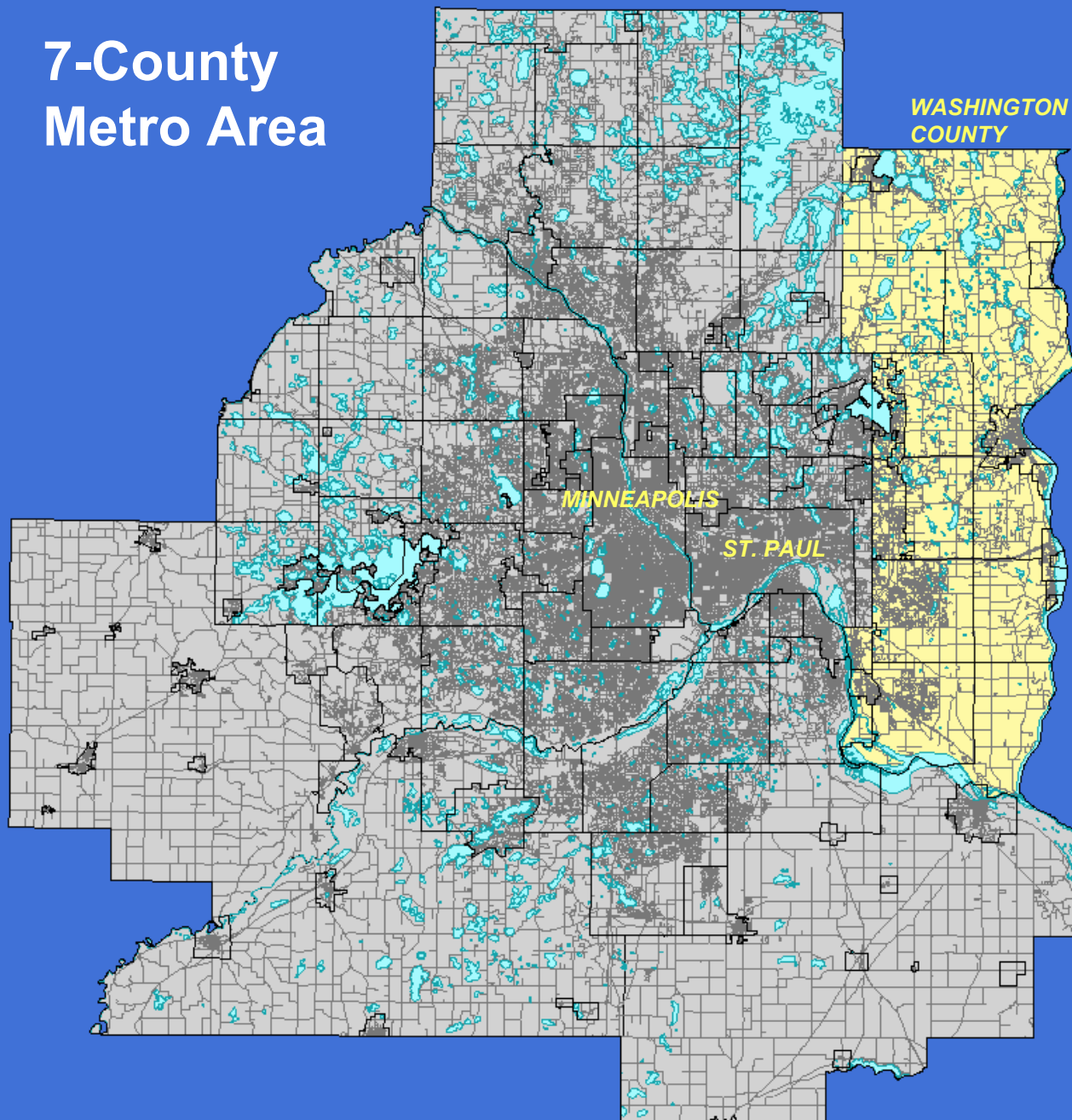
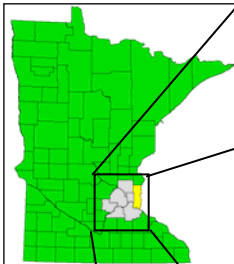
- Issues of aquifer “sustainability” (driven by population growth)
- Quantifying predictions of effects of development and changes in land use
- Requirements for “zero-discharge” development
- Quantifying recharge augmentation
- Climate change issues

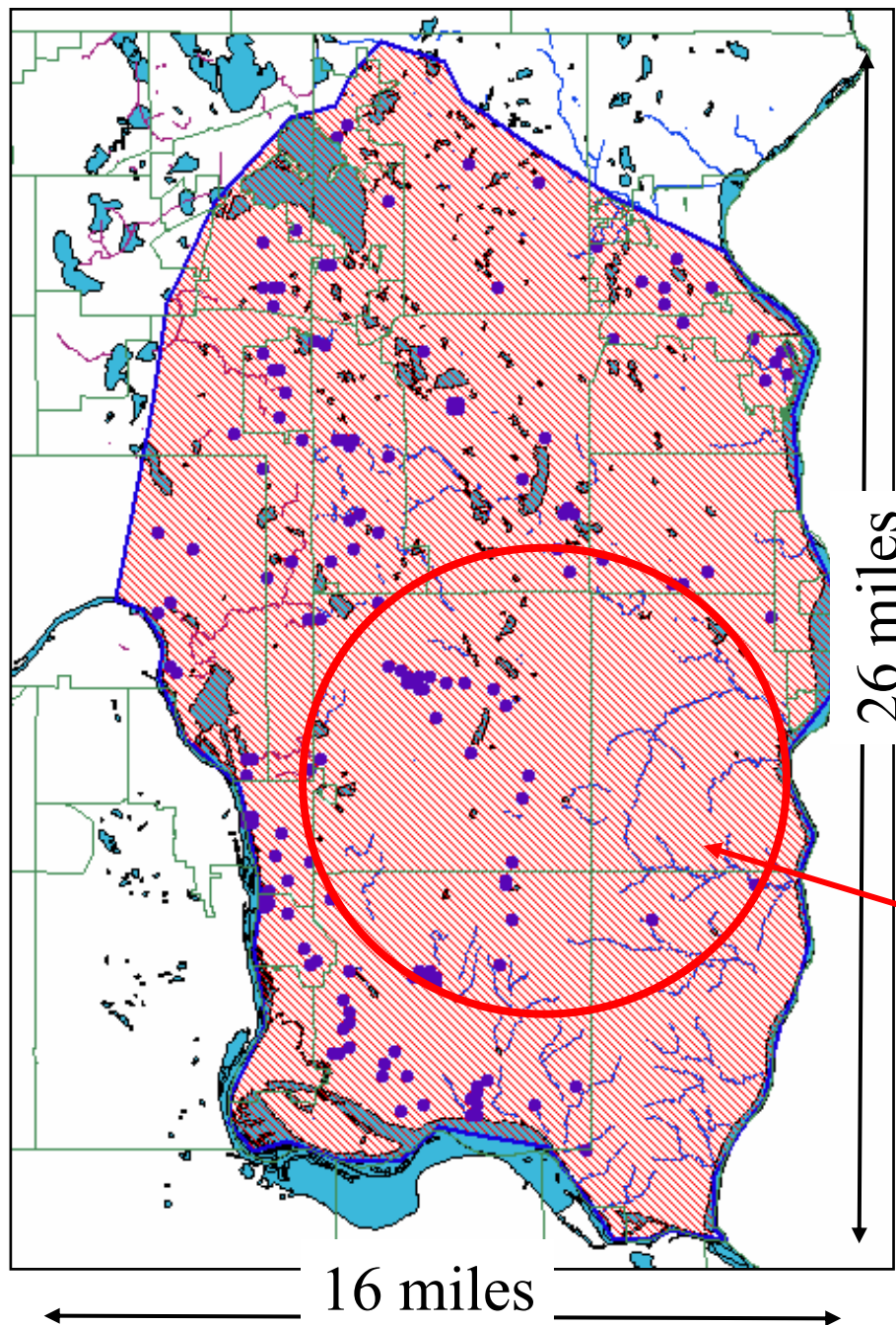
These types of issues are leading toward expectations of quantifying recharge rates and smaller and smaller scales

# **Infiltration (Recharge) Derived from Deterministic Modeling of Surface Processes**

Infiltration = Water that moves from the ground surface to the saturated zone and becomes groundwater

# 7-County Metro Area



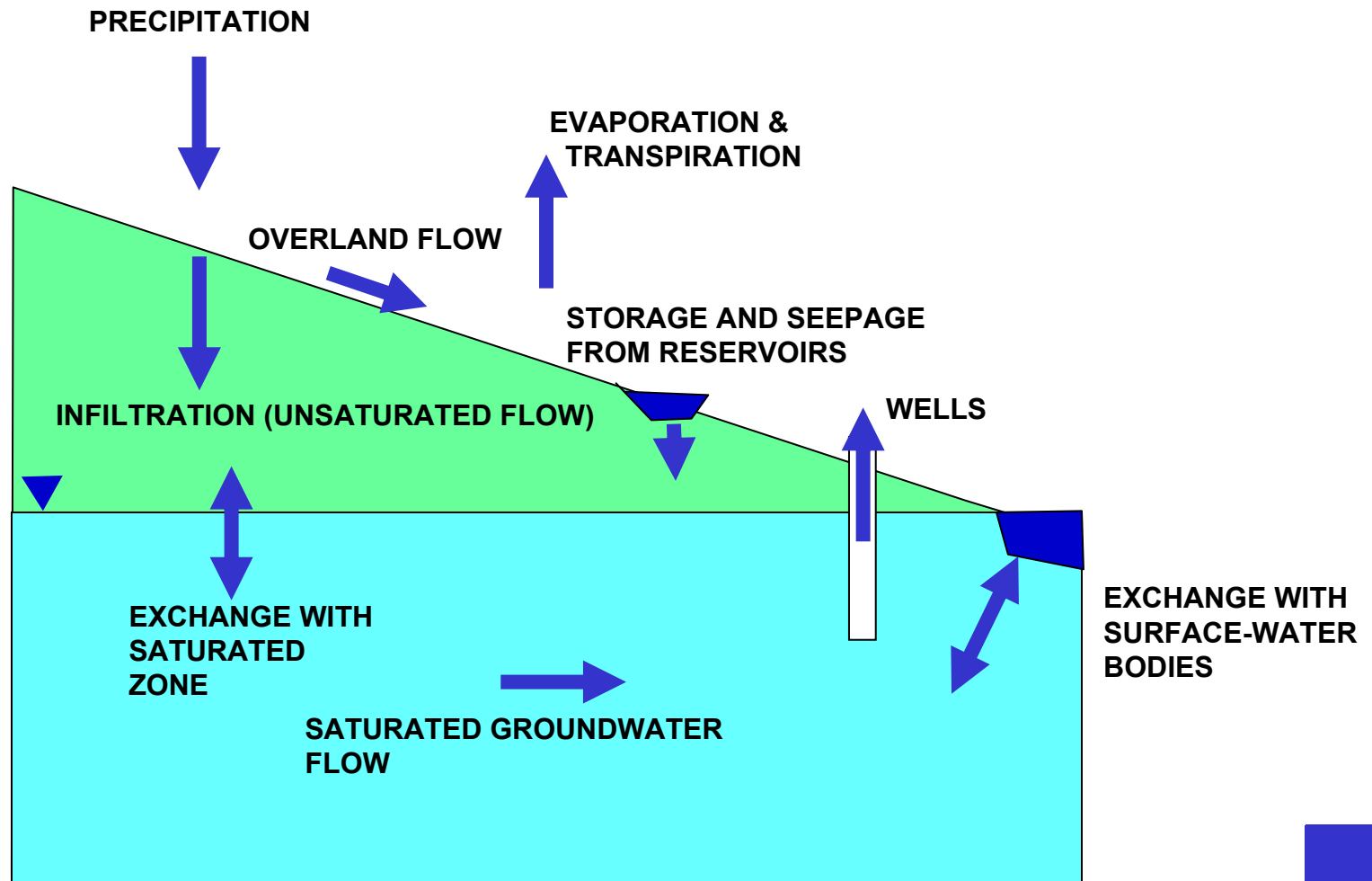


## The Areas of interest

primary area of interest



# Conceptual Model of Processes

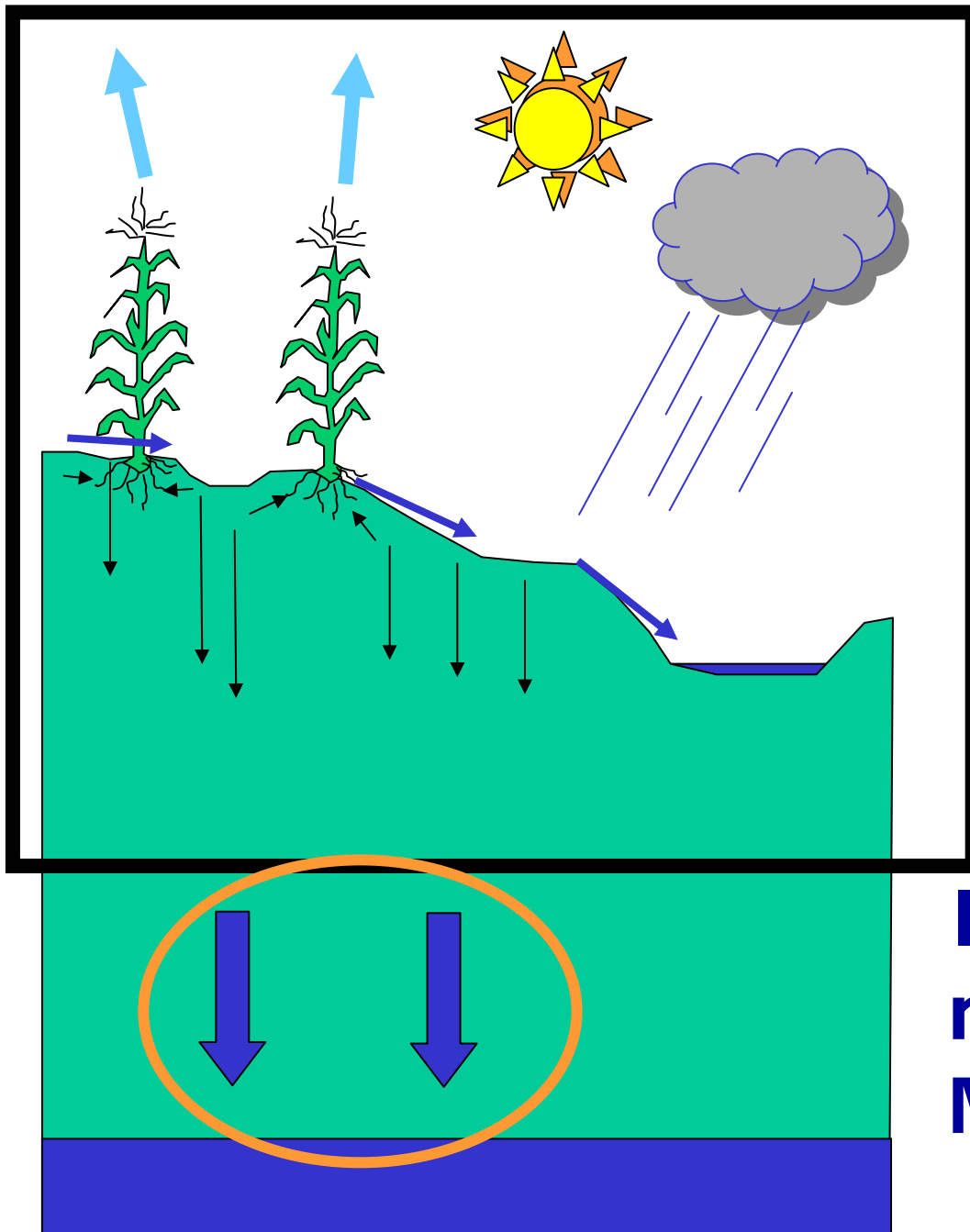


# What is MIKE SHE

- MIKE SHE is *several* models, brought together into a single Graphical User Interface (GUI)
- Is capable of simulating:
  - precipitation
  - Evaporation (soil, free-water, and canopy)
  - transpiration
  - overland flow
  - channel flow
  - unsaturated flow
  - saturated flow

# Why was MIKE SHE used?

- To obtain deterministic, distributed, climate and land-use based infiltration rates
- To constrain optimization and reduce parameter correlation in calibration
- To estimate infiltration for normal and dry conditions

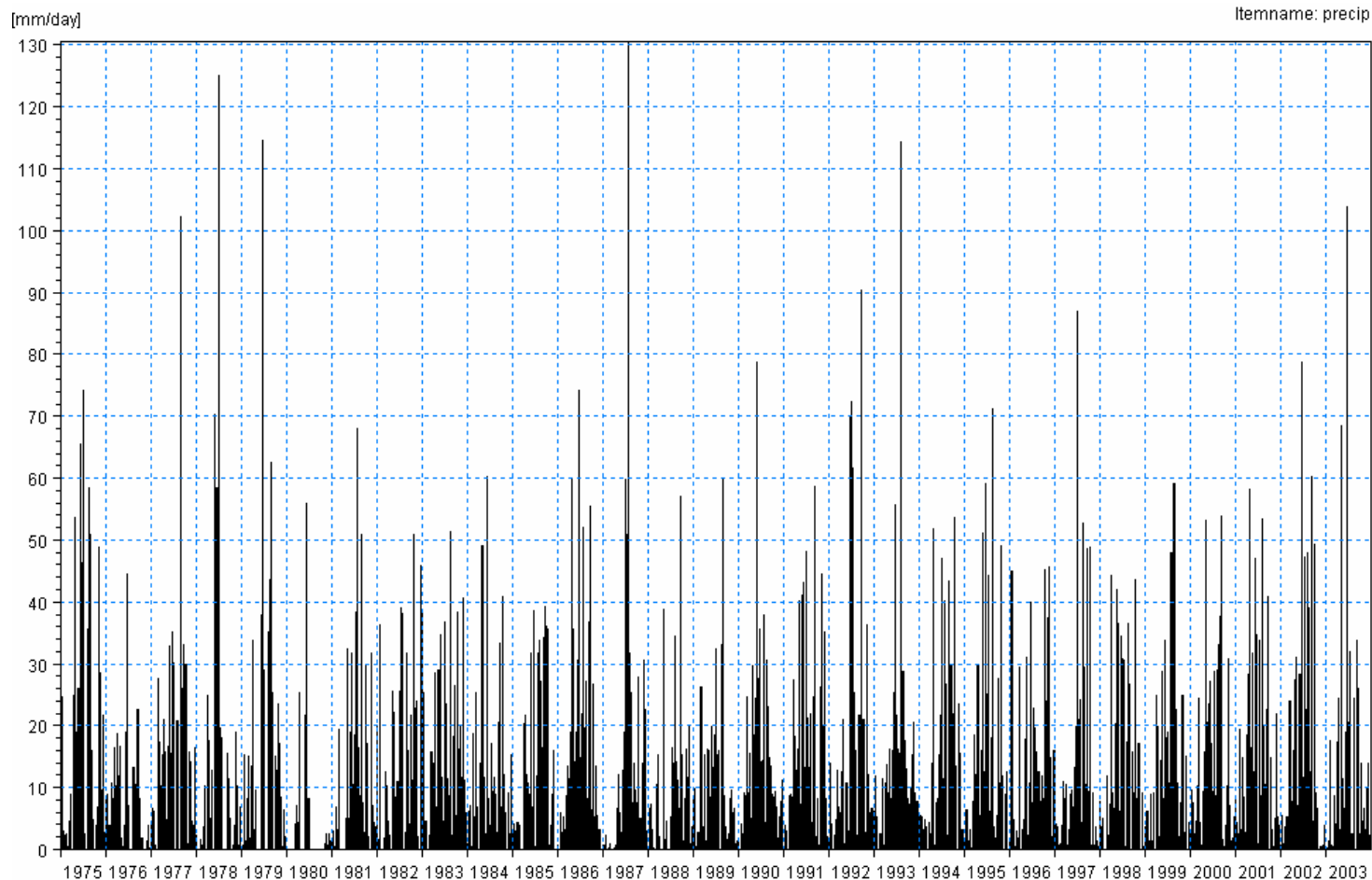


**MIKE SHE  
Processes**

**Infiltration  
rates to  
MODFLOW**

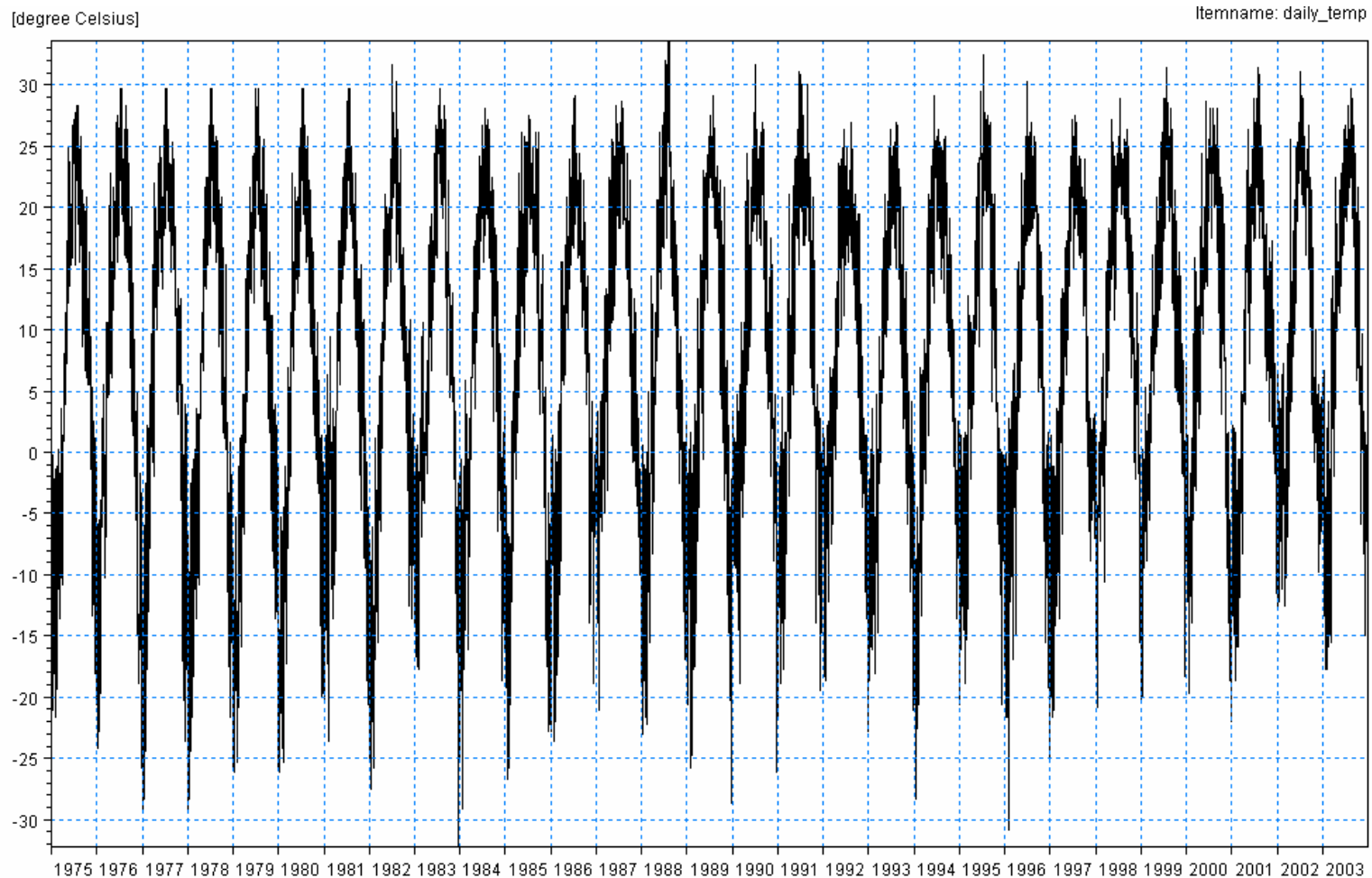
# 1. Precipitation

## Daily Precipitation Data from St. Paul Metro Site (1975-2003)



## 2. Temperature

### Mean Daily Temp (C) from St. Paul Metro Site (1975-2003)

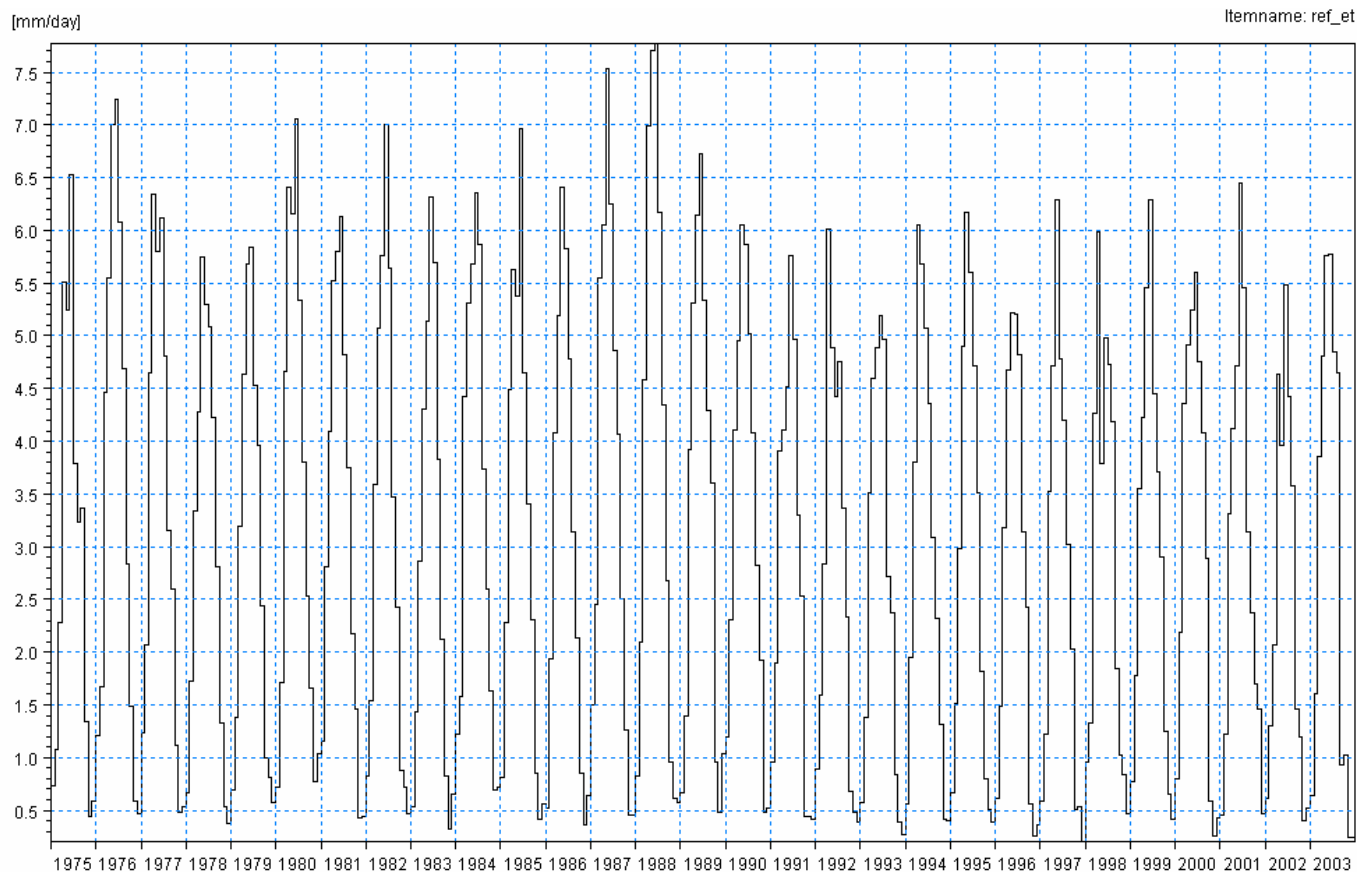


# Temperature is used to...

- Determine if precipitation is stored as snow
- Determine when melting of snow pack begins
- Used in evaporation and transpiration calculations

# 3. Reference Evapotranspiration

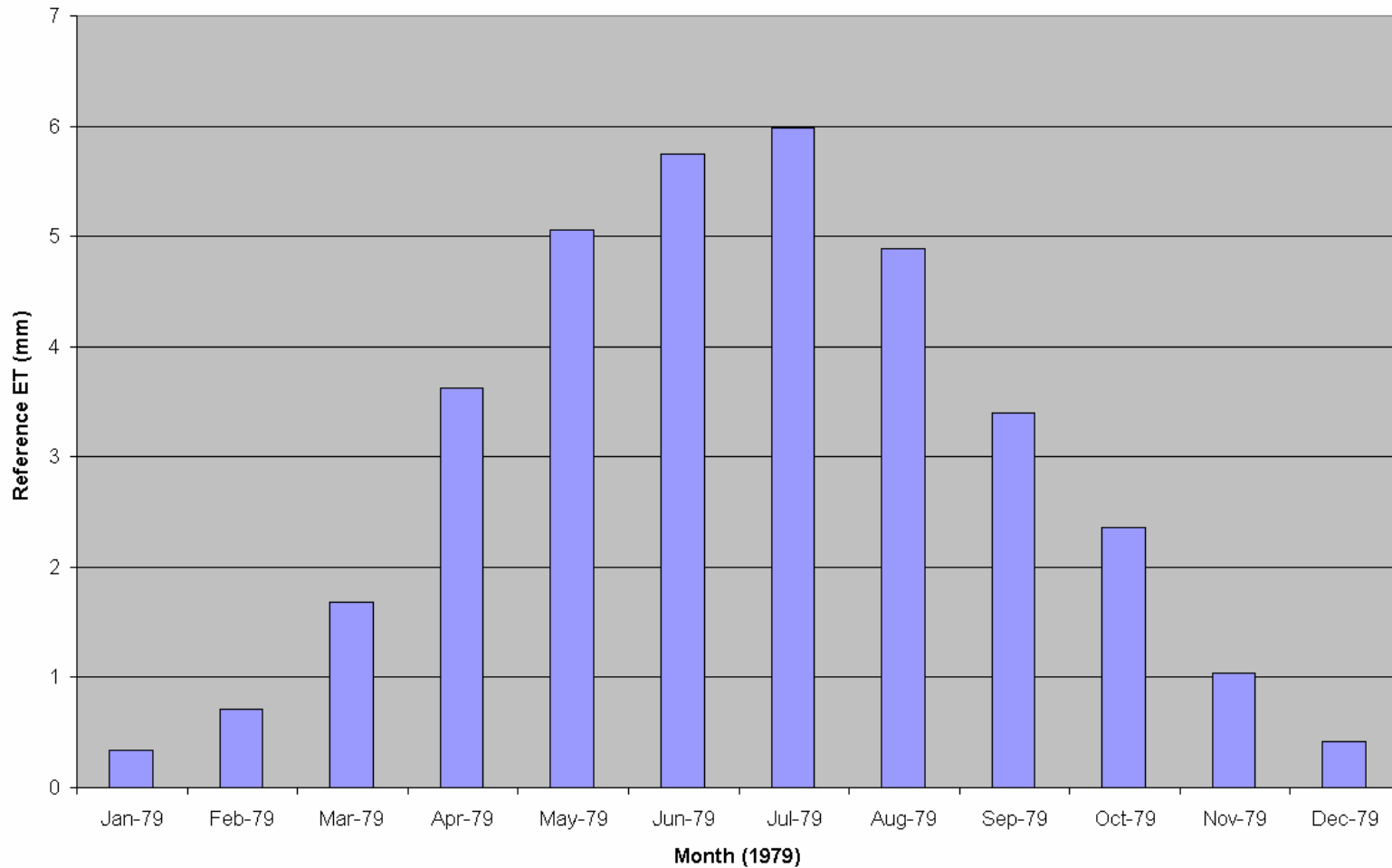
**Reference ET: “a hypothetical reference crop with an assumed crop height of 0.12 m, a fixed surface resistance of 70 s/m and an albedo of 0.23”**





# Monthly variations in Reference ET

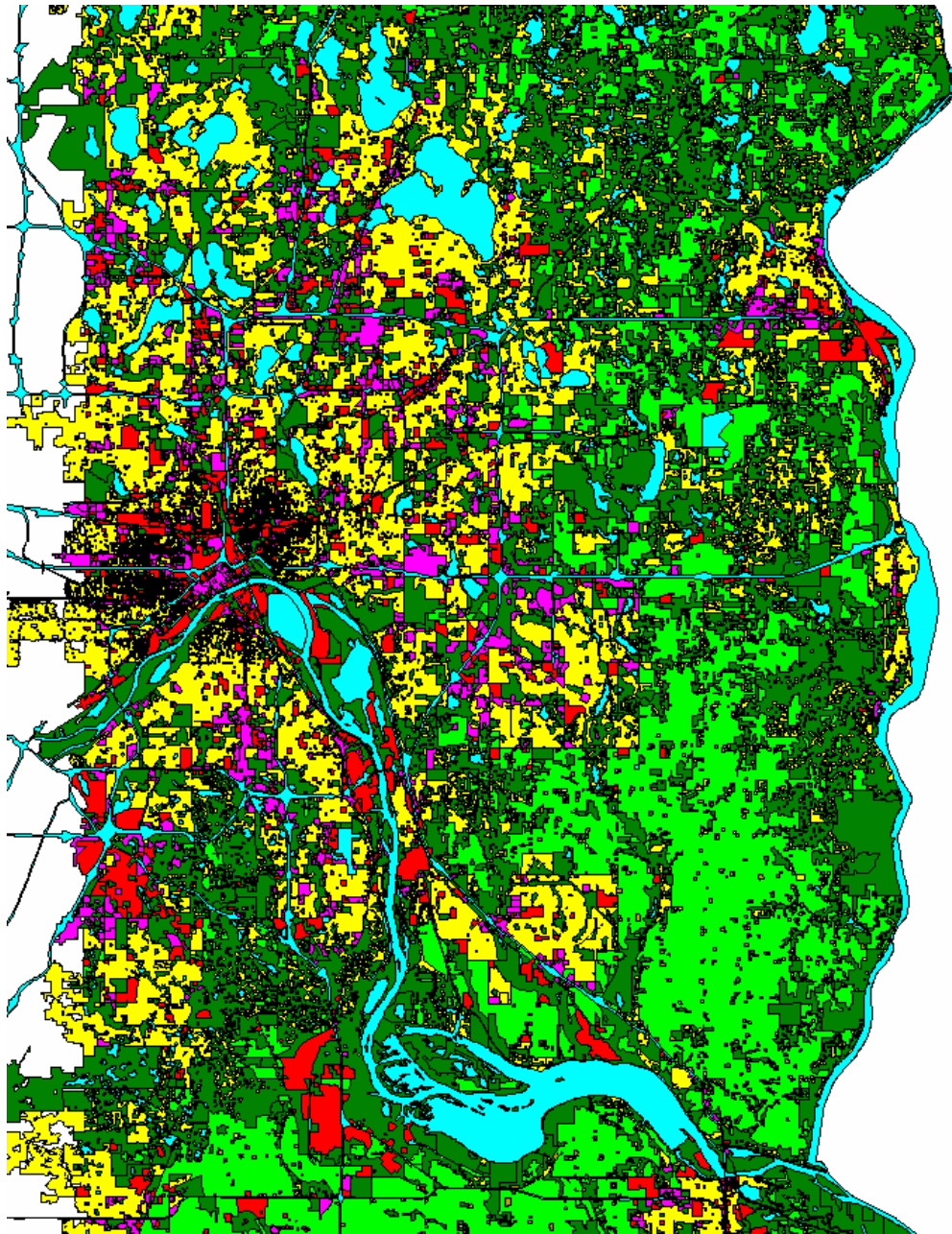
Calculated Monthly Reference ET










# Factors included in Reference ET

- Latitude & Day and Month (sun angle)
- Mean daily wind speed
- Minimum and Maximum Temperature
- Dew Point/Relative Humidity
- Percent cloud cover

calculation methods source: <http://www.fao.org> chapters 2 and 3



## 4. Land Use/Vegetation

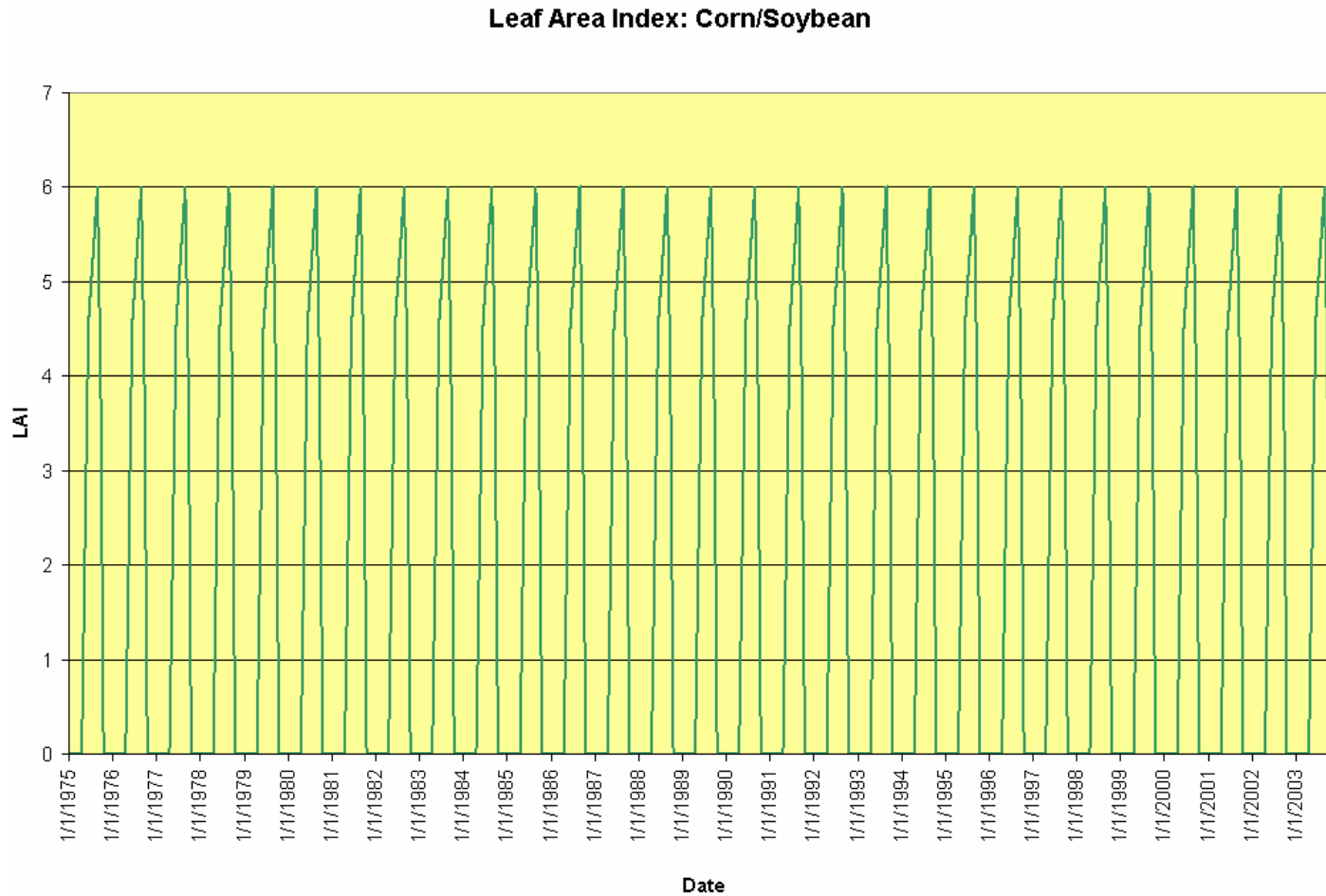
	CORN/SOY BEAN
	SINGLE FAMILY RESIDENTIAL
	COMMERCIAL
	INDUSTRIAL
	FARMSTEADS
	PARK LAND
	OPEN WATER & PAVED

For each vegetation type, a “Leaf Area Index” (LAI) and “Rooting Depth” were estimated

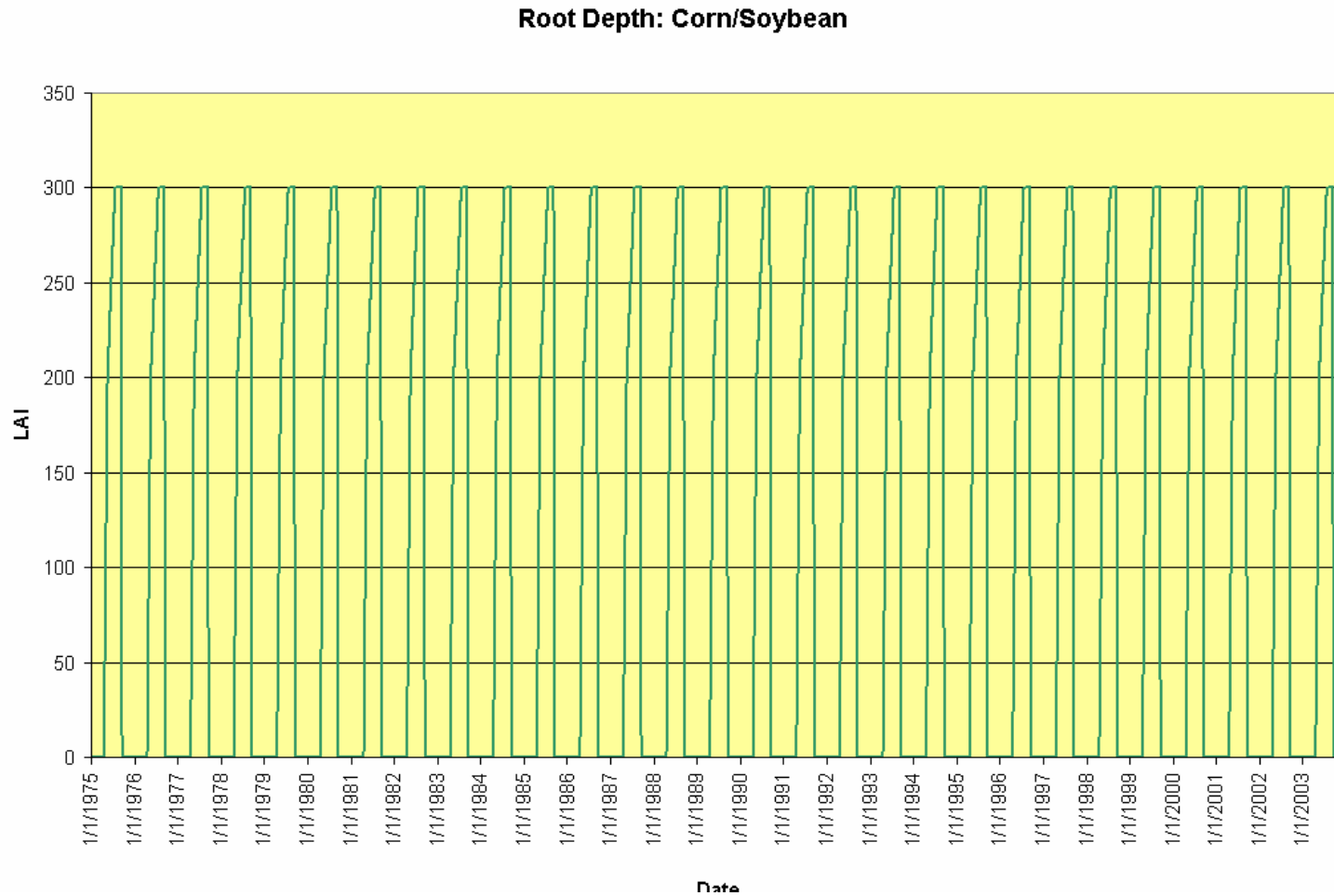
# Leaf Area Index Example

source: [http://www-eosdis.ornl.gov/vegetation/lai\\_support\\_images.html](http://www-eosdis.ornl.gov/vegetation/lai_support_images.html)

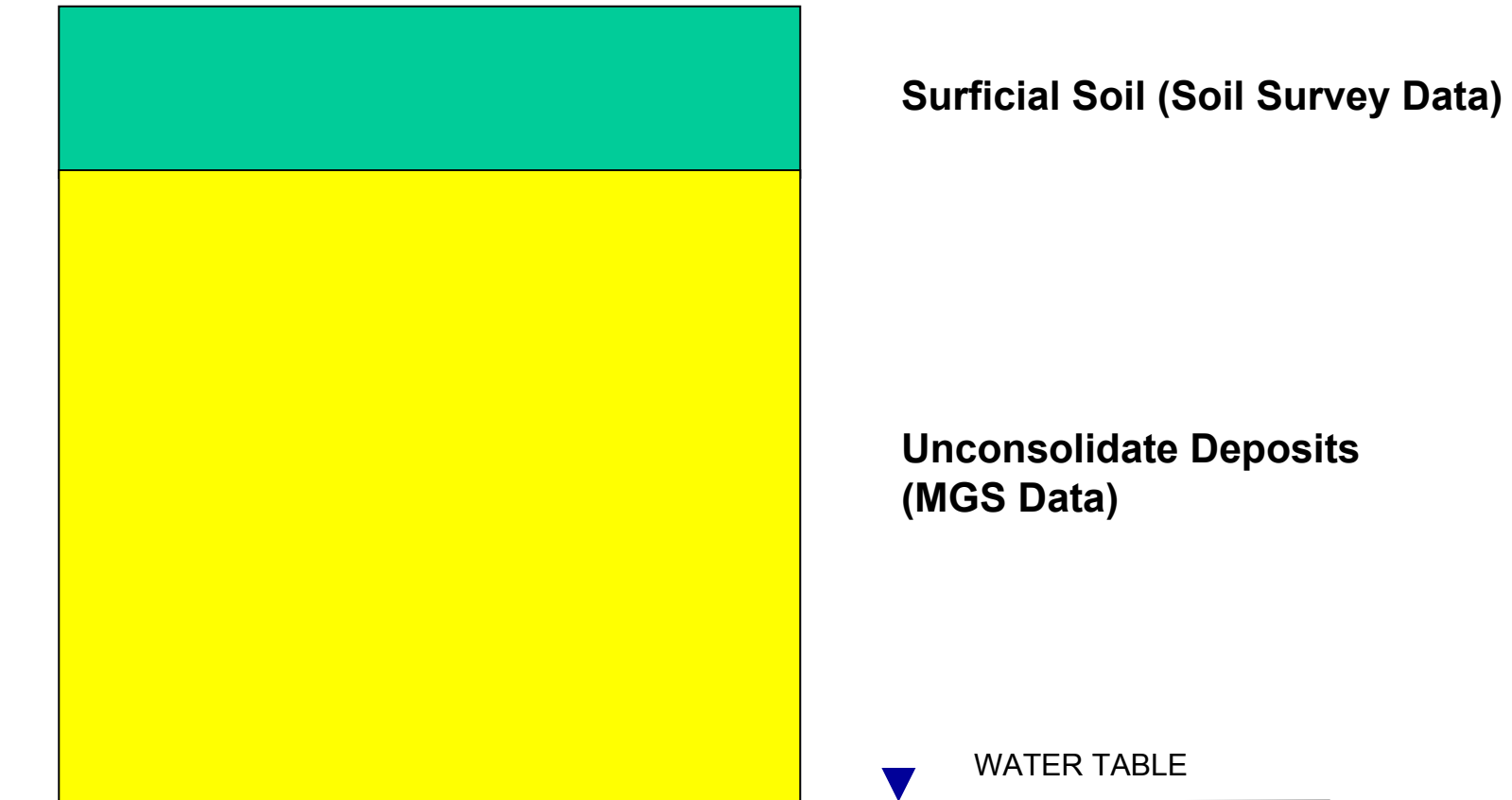
“global leaf area index data from field measurements, 1932-2000, summary table



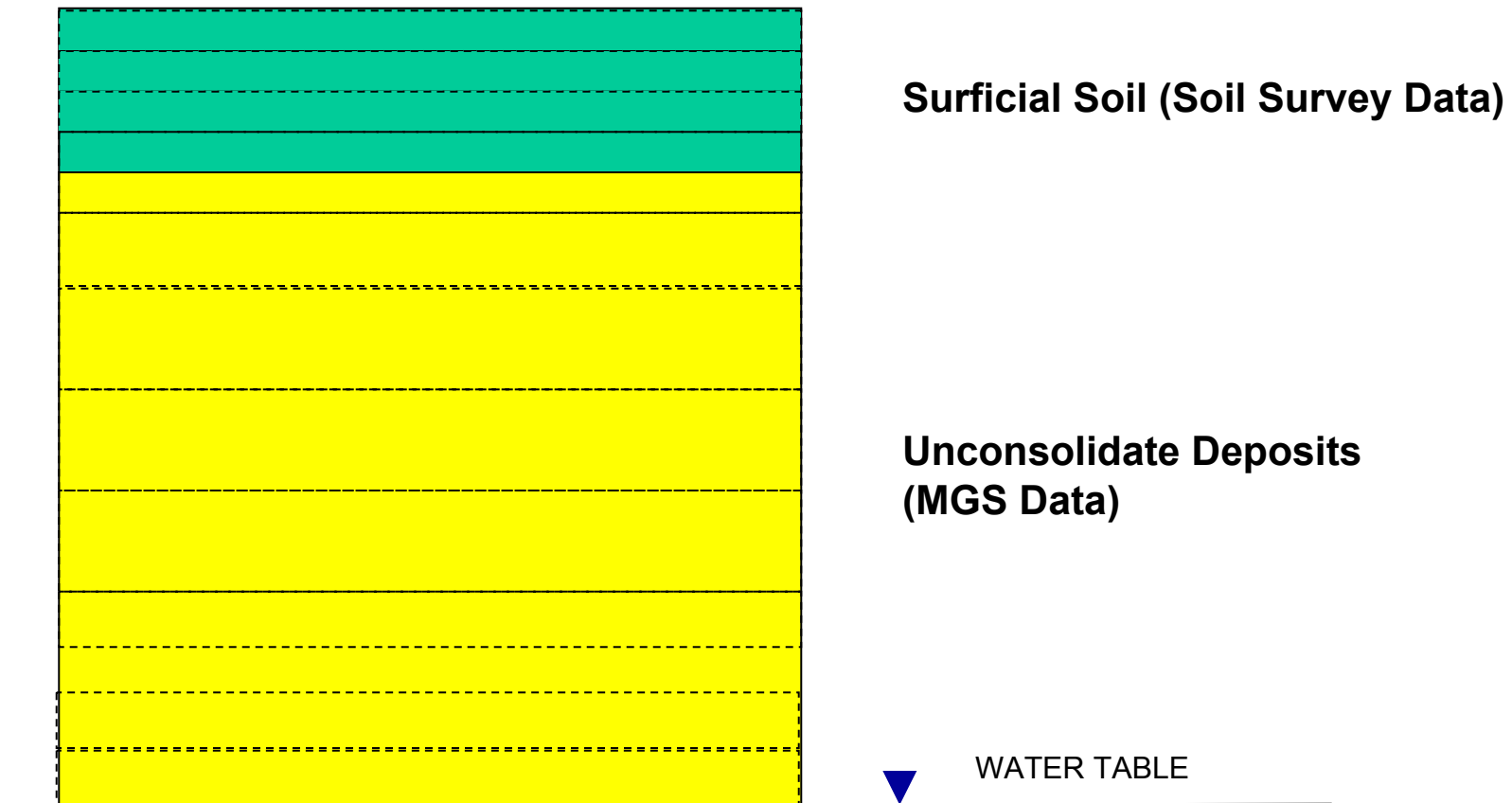
# Root Depth Example



## 5. Vadose Zone Profile



# Computation Layers in Vadose Zone



# Unsaturated Flow Uses Richards Equation

$$\frac{d\theta}{dt} = \frac{d}{dx} K \left( \frac{d\Psi}{dx} + \frac{dz}{dx} \right) + S$$

this says:

volumetric moisture content ( $\theta$ ) changes over time as a function of:

$\Psi$  (the matric potential, which is a function of soil type)

$K$  (hydraulic conductivity, which also changes with matric potential)

$S$ , which is the input or output of water from the soil (e.g, infiltration, ET)

This is a very non-linear, difficult to solve problem  
without making simplifications



**The most important consideration is relating Hydraulic Conductivity to moisture content**

$$K(\Psi) = K_s \frac{((1 + |\alpha\Psi|^n))^m - |\alpha\Psi|^{n-1})^2}{(1 + |\alpha\Psi|^n)^{m(l+2)}}$$

Van Genuchten Equation  
(an approximation)

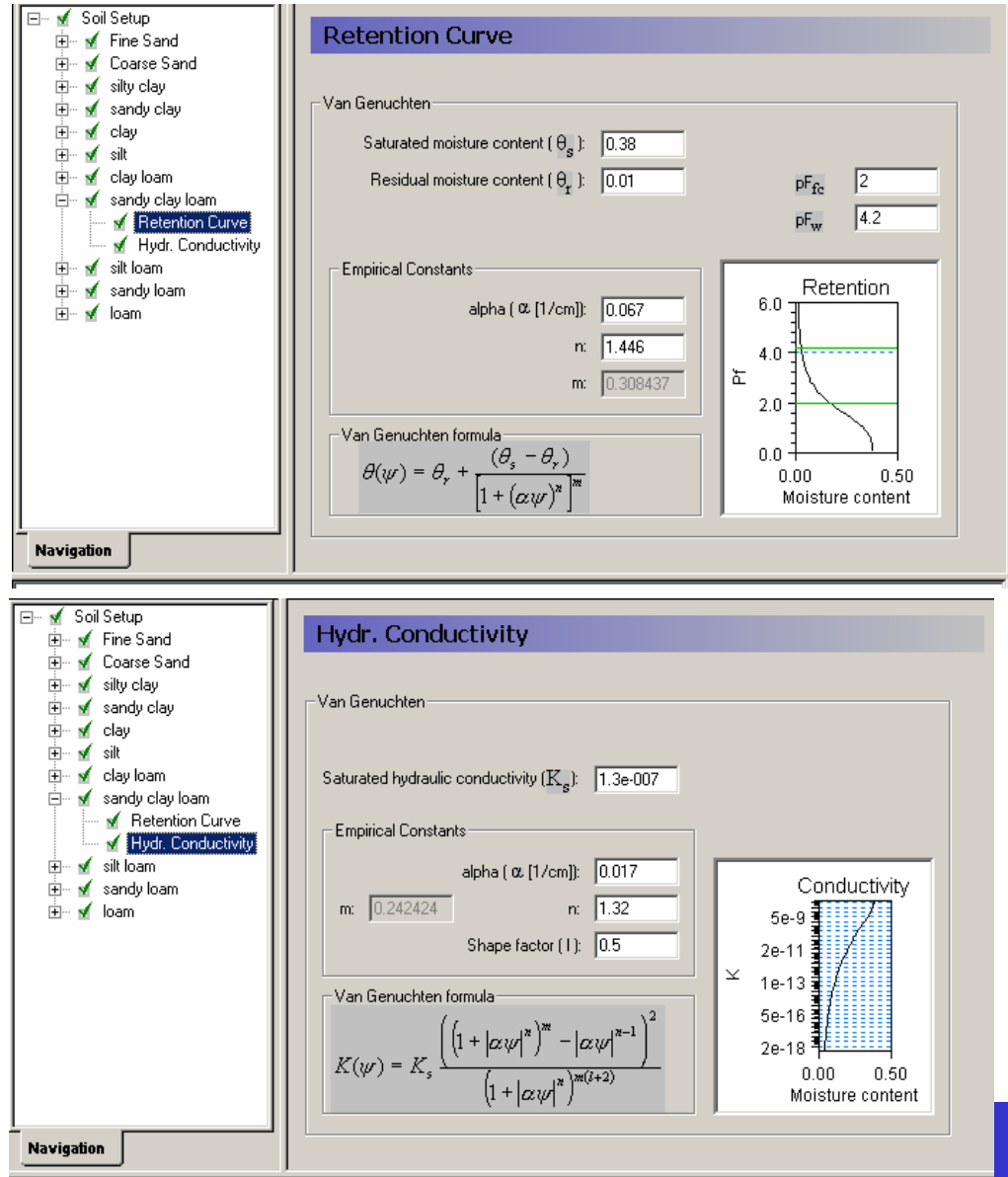
# Large-scale values for the Van Genuchten variables were obtained for various soil types

	$\alpha(1/\text{cm})$	$n$	$K_s \text{ (m/s)}$	$m$
Silty clay	0.013	1.32	7.13E-09	0.242
sandy clay	0.032	1.20	1.23E-08	0.167
clay	0.015	1.26	1.35E-09	0.206
silt	0.006	1.65	1.90E-07	0.394
clay loam	0.015	1.40	1.05E-08	0.286
sandy clay loam	0.017	1.32	1.30E-07	0.242
silt loam	0.005	1.65	1.46E-07	0.394
sandy loam	0.022	1.50	7.83E-07	0.333
loam	0.011	1.50	5.25E-07	0.333
sand	0.030	2.90	3.25E-06	0.655

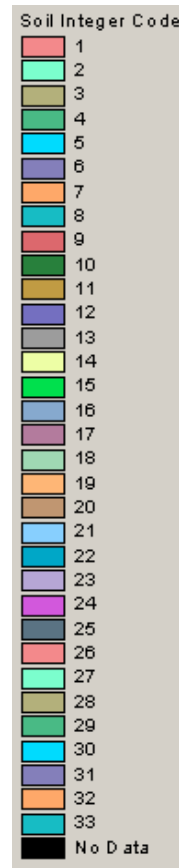
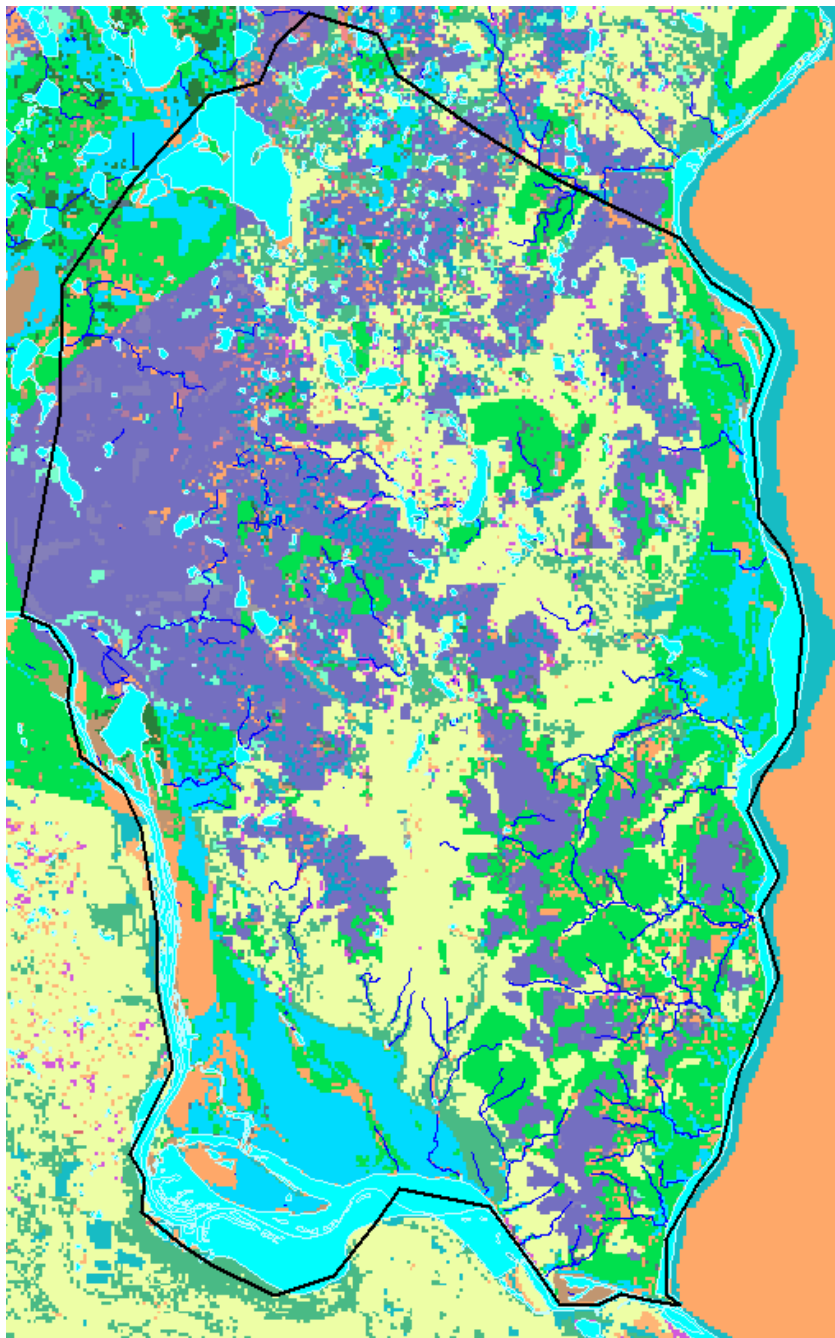
Zhu, J., and B.P. Mohanty. Spatial Averaging of van Genuchten Hydraulic Parameters for Steady State Flow in Heterogeneous Soils. *Vadose Zone Journal*. 1:261-271, 2002.

# Soil Retention Curve and K sat Curve Developed for the 9 Soil Types

- Fine Sand
- Coarse Sand
- Silty Clay
- Clay
- Silt
- Clay Loam
- Sandy Clay Loam
- Silt Loam
- Loam



# Soil Grid Integer Code



Synthesis of surface soil data  
and surficial geology data (above  
water table)

Arcgrid: soil\_id

## UZ Soil Profile Definition

Profile ID:  Grid code value:

Soil Profile:

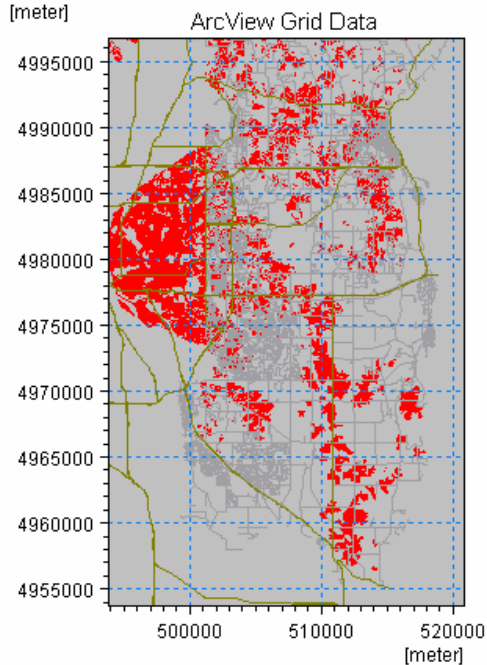
	From depth	To depth	Soil name	UZ Soil property file		
1	0	1	silt loam	V:\23\...\unsat\surficial_deposits.U	...	Edit...
2	1	100	sandy clay	V:\23\...\unsat\surficial_deposits.U	...	Edit...

Vertical Discretization:

	From depth	To depth	Cell height	No of cells
1	0	1	0.2	5
2	1	4	0.5	6
3	4	100	4	24

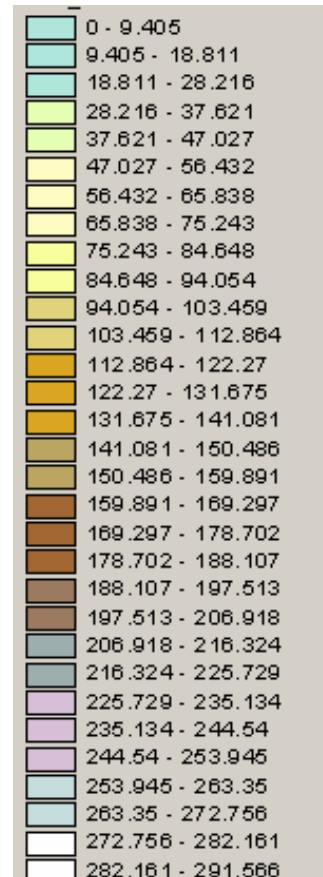
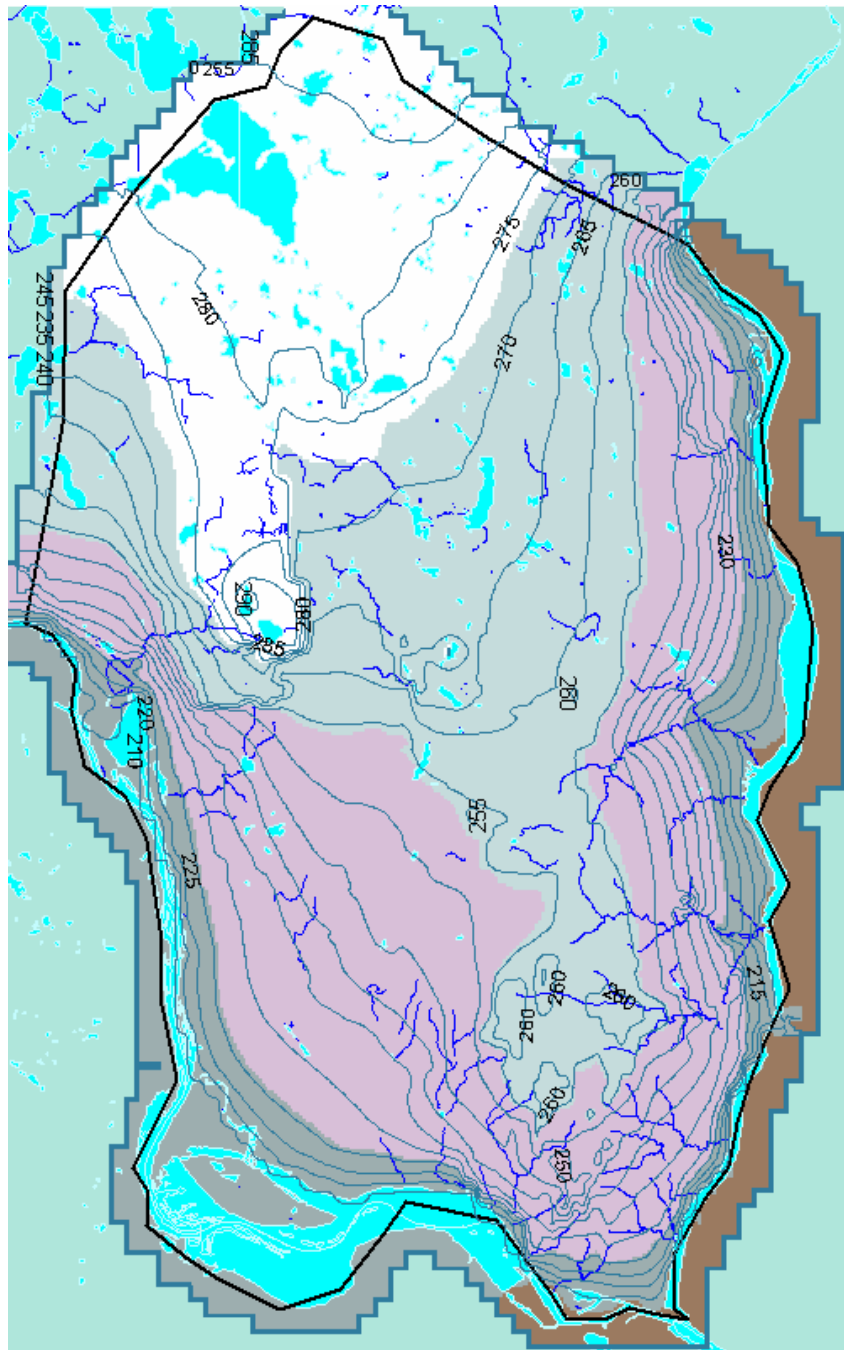
Bypass Const.

byp   
thr1   
thr2



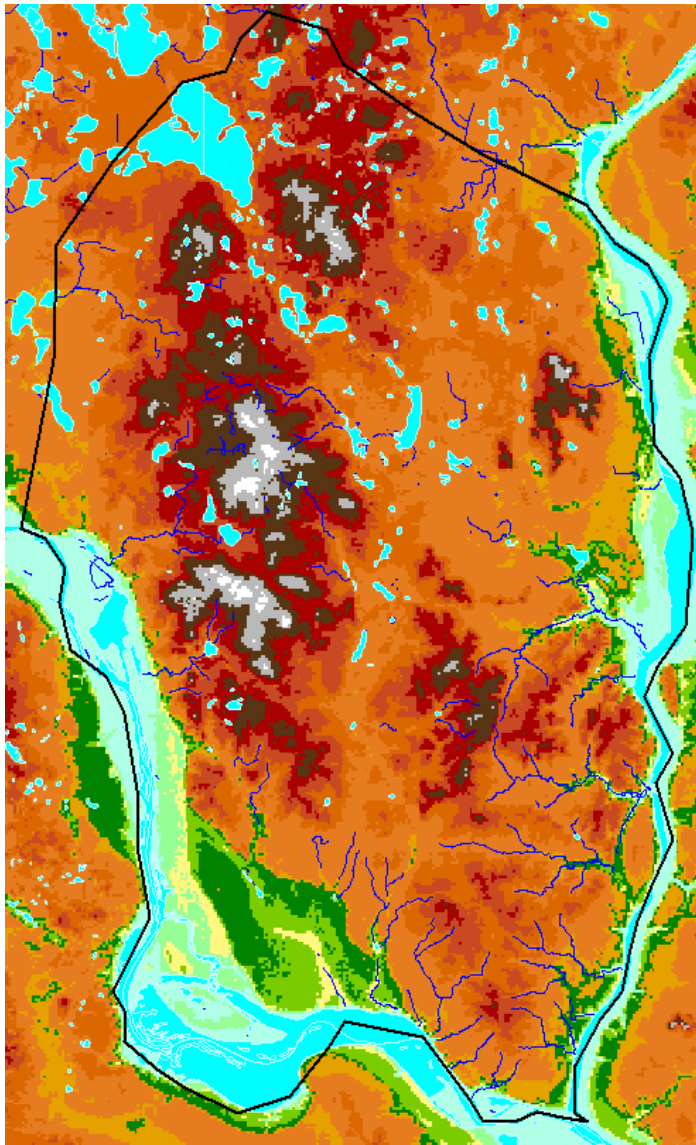
## Soil Profile Definitions for Each Grid Code

# Water-Table Surface for MIKE SHE Computations



Arcgrid: wat\_tab

## 6. Overland Flow



**100-m grid ground  
surface elevation (m,  
MSL)**

	202 - 211
	211 - 220
	220 - 229
	229 - 237
	237 - 246
	246 - 255
	255 - 264
	264 - 273
	273 - 282
	282 - 291
	291 - 300
	300 - 308
	308 - 317
	317 - 326
	326 - 335
	No Data

Calculated from:

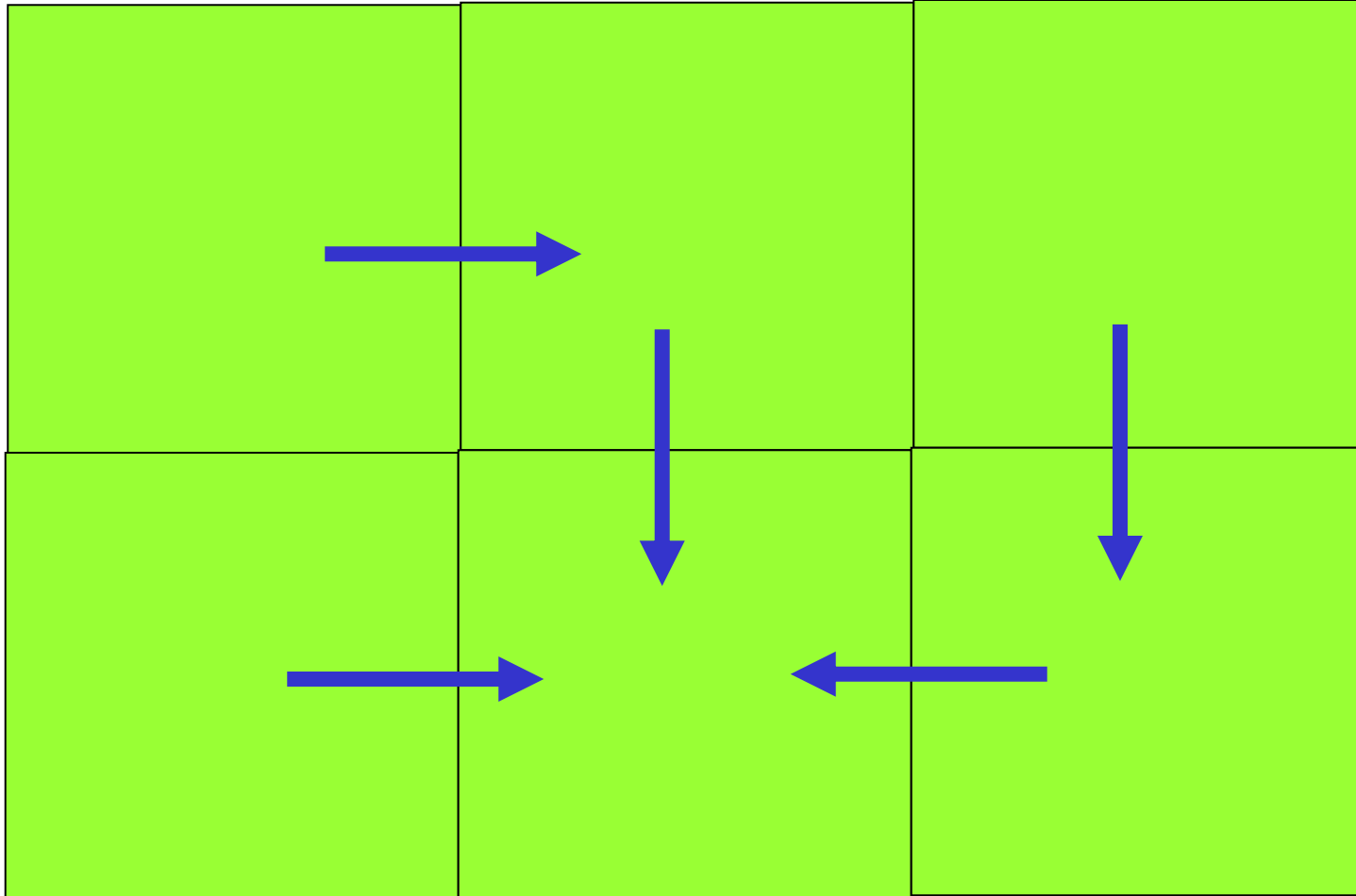
1. 20-m grid of Washington Co.
2. DEM (30-m)

# Overland Flow Computations

- Uniform Manning Number ( $1.5 \text{ m}^{1/3}/\text{S}$ )
- Water depth threshold to initiate overland flow = 0.2 meters (based on topography and grid)



# Overland Flow Routing is by Grid Cells



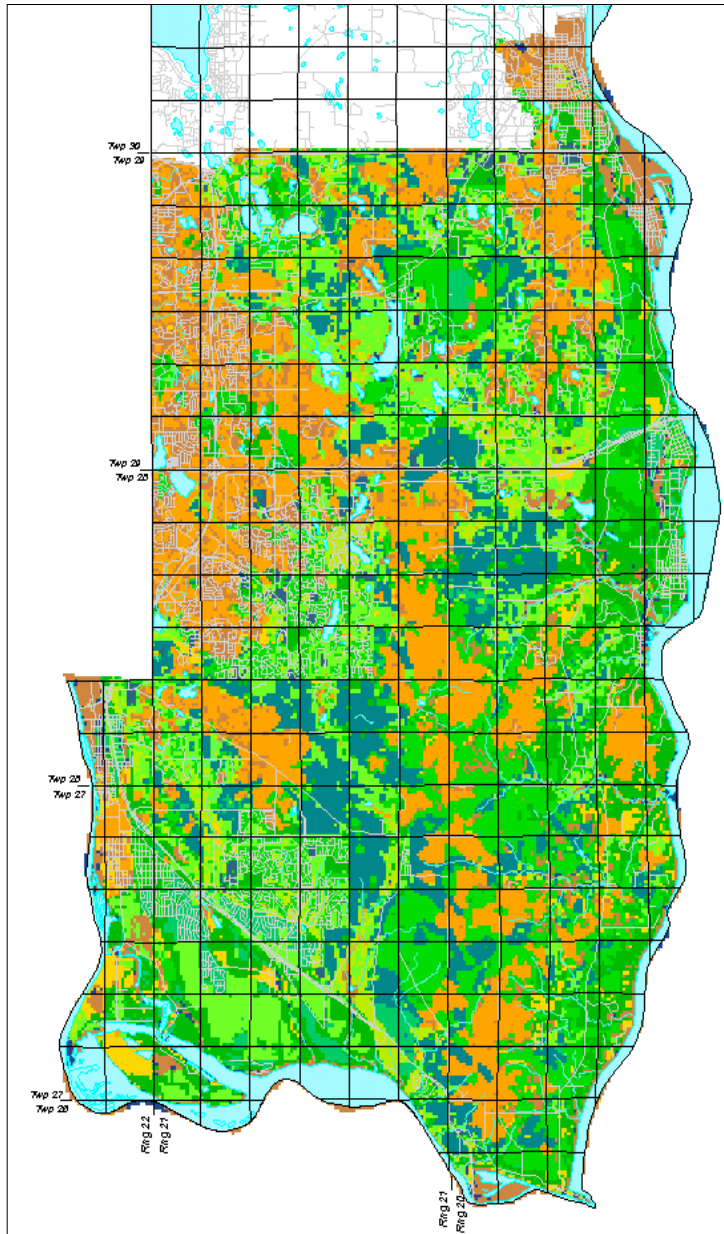
# Running MIKE SHE to obtain infiltration

- Adaptive time stepping, based on precip and overland flow constraints (typically 12 minutes to 4 hours)
- Simulations for 1979-2003 took 6.5 days of continuous CPU time
- Channel flow (MIKE 11) set up but not in use (topography controls flow)
- Water table stationary (decoupled with saturated zone)

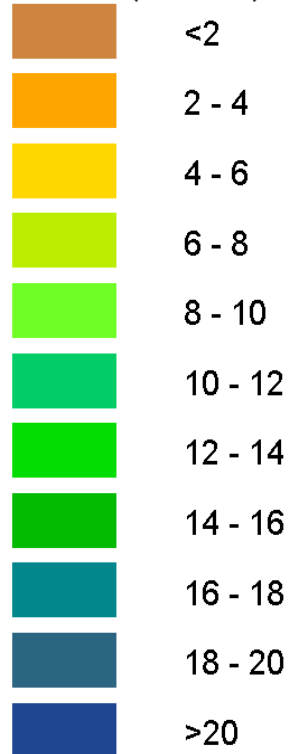
# MIKE SHE Results

- Focused primarily on time-dependent exchange between saturated and unsaturated zone (i.e. recharge)
- Negative values do occur (ET pulling from capillary fringe)
- For MODFLOW model input, mean accumulated exchange calculated for calendar months

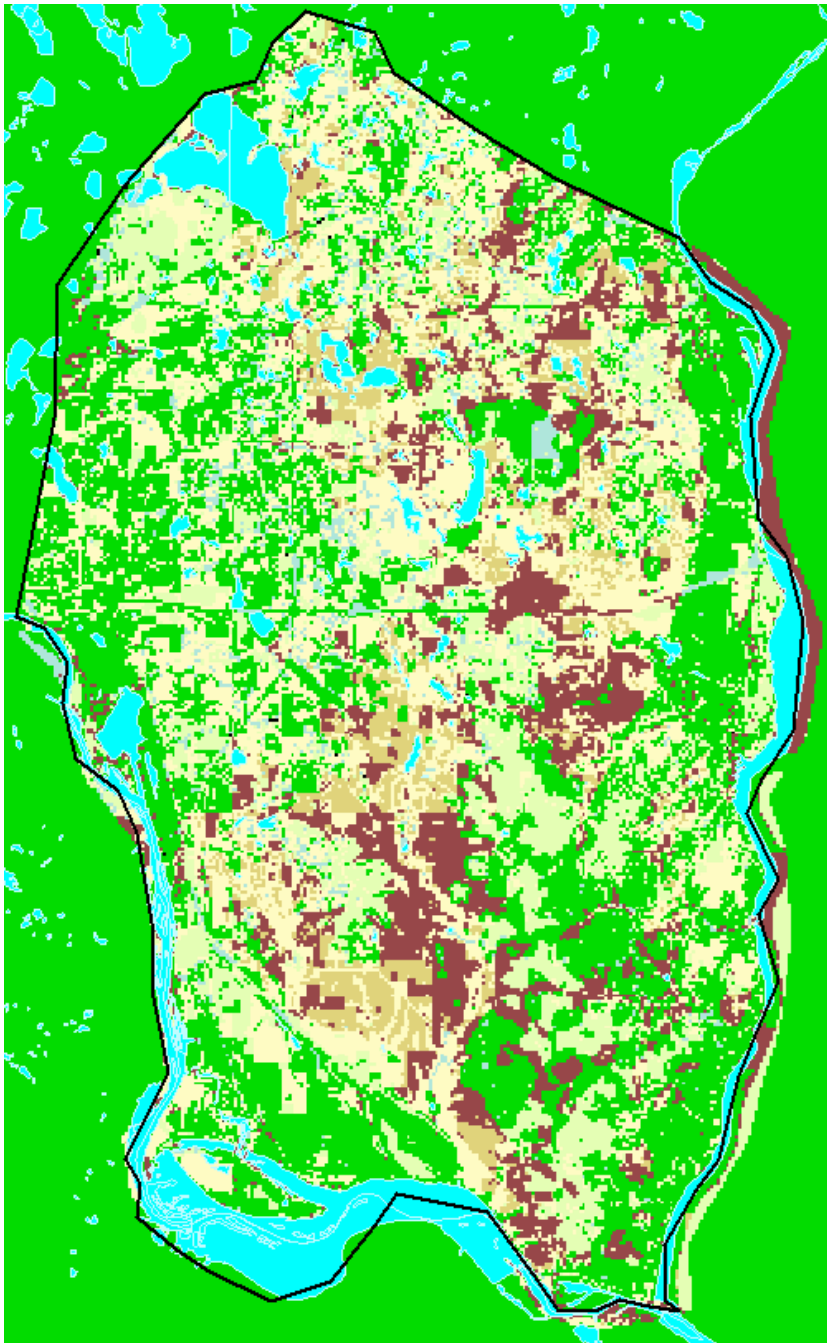
# Average Recharge: 1979-2002



Average Annual  
Infiltration (inches)



Areally Averaged  
Rate = 8.67 in/yr









## Difference in Annual Infiltration: Average vs 1988

1988 Annual total/model domain = 6.67 in/yr

Average Annual total/model domain = 8.67 in/yr

in/year

	-1 - 0
	0 - 1
	1 - 2
	2 - 3
	3 - 4
	> 4

positive values indicate  
more infiltration during Average  
year

## **This method... (the ugly)**

- Is very data intensive
- Is very computationally intensive
- Is not calibrated and not verified in this application
- Is a vast simplification of many very complex processes

# **This method... (the not so ugly)**

- Is based primarily on precipitation and land use/land form (not aquifer characteristics and water levels)
- Ties recharge to land use and soil characteristics
- Is sensitive to climatic conditions
- Can be used with data available for the metro area
- Is a vast simplification of many very complex processes